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## Geometry Second Semester Final Exam Review

1. Find the length of the leg of this right triangle. Give an approximation to 3 decimal places.

2. Find the length of the leg of this right triangle. Give an approximation to 3 decimal places.

a. 8.062
b. $\quad 17.748$
c. 46.098
d. 18.028
3. How long is a string reaching from the top of a $12-\mathrm{ft}$ pole to a point on the ground that is 6 ft from the bottom of the pole? Give an exact answer and an approximation to 3 decimal places.
4. A 25.5 foot ladder rests against the side of a house at a point 24.1 feet above the ground. The foot of the ladder is $x$ feet from the house. Find the value of $x$ to one decimal place.

a. 1.9
b. 7.0
c. 8.3
d. $\quad 10.1$
5. Find $a, b$, and $h$.

6. Find the length of the altitude drawn to the hypotenuse.

7. Find the value of $x$.

a. $3 \sqrt{2}$
b. $3 \sqrt{6}$
c. $3 \sqrt{5}$
d. $3 \sqrt{30}$
8. Find the value of the variable in the diagram.

9. Find the value of $x$ and $y$.
10. Find the value of $x$ and $y$.

11. Find the value of $x$.

12. Find $\tan A$ for the right triangle below:

13. Explain how a tangent ratio can be used to find the height of the building in the figure below. Find the height of the building when $\angle A=35^{\circ}$.


14. A photographer shines a camera light at a particular painting forming an angle of $47^{\circ}$ with the camera platform. If the light is 52 feet from the wall where the painting hangs, how high above the platform is the painting?

a. $\quad 0.93 \mathrm{ft}$
b. 55.76 ft
c. $\quad 1.07 \mathrm{ft}$
d. $\quad 48.49 \mathrm{ft}$
15. Find $\sin P, \cos P, \tan P$.

16. Write the trigonometric ratio.
A. $\sin A$
B. $\tan B$

17. A slide 4.4 m long makes an angle of $33^{\circ}$ with the ground. How high is the top of the slide above the ground?
a. $\quad 2.53 \mathrm{~m}$
b. 2.4 m
c. $\quad 3.69 \mathrm{~m}$
d. $\quad 2.86 \mathrm{~m}$
18. Liola drives 19 km up a hill that is at a grade of $15^{\circ}$. What horizontal distance, to the nearest tenth of kilometer, has she covered?
a. $\quad 5.1 \mathrm{~km}$
b. $\quad 4.9 \mathrm{~km}$
c. $\quad 14.2 \mathrm{~km}$
d. $\quad 18.4 \mathrm{~km}$
19. Find the value of $x$, to the nearest whole number. (not drawn to scale)

20. Find $x$, to the nearest hundredth.

21. Solve the right triangle: $\alpha=20^{\circ}$ and $a=20$; Find $\beta, b$, and $c$.

22. Find the missing angle and side measures of $\triangle A B C$, given that $\mathrm{m} \angle A=20^{\circ}, \mathrm{m} \angle C=90^{\circ}$, and $C B=20$.
a. $\mathrm{m} \angle B=110^{\circ}, c=58.5, b=55.4$
b. $\quad \mathrm{m} \angle B=70^{\circ}, c=59, b=54.9$
c. $\mathrm{m} \angle B=70^{\circ}, c=58.5, b=54.9$
d. $\mathrm{m} \angle B=110^{\circ}, c=58.5, b=54.9$
23. Two legs of a right triangle have lengths 15 and 8 . The measure of the smaller acute angle is
$\qquad$ _.
a. $\approx 32.2^{\circ}$
b. $\approx 17^{\circ}$
c. $\approx 61.9^{\circ}$
d. $\approx 28.1^{\circ}$
24. An airplane is flying at an elevation of 1500 feet. What is the airplane's angle of elevation from the runway when it is 5000 feet from the runway? Explain.

25. An antenna is atop the roof of a 100 -foot building, 10 feet from the edge, as shown in the figure below. From a point 50 feet from the base of the building, the angle from ground level to the top of the antenna is $66^{\circ}$. Find $x$, the height of the antenna, to the nearest foot.

26. The translation vector is $\vec{u}=\langle-7,4\rangle$. If the image of $A$ is $A^{\prime}(6,-4)$, find the coordinates of point $A$.
27. The translation vector is $\vec{u}=\langle 7,-3\rangle$. The image of point $A$ is $A^{\prime}(5,-7)$. Find the coordinates of $A$.
28. The point $A(-7,3)$ is translated onto $A^{\prime}$ by the vector $\vec{u}=\langle 5,-4\rangle$. The coordinates of $A^{\prime}$ are
a. $(-2,-1)$
b. $(-12,7)$
c. $(2,-7)$
d. $(5,-4)$
29. The points in a coordinate plane are reflected in the $y$-axis. In general, every point $(x, y)$ is mapped onto what point?
30. The points in a coordinate plane are reflected in the line $y=x$. In general, every point $(x, y)$ is mapped onto what point?
31. Suppose the triangle in the figure below is reflected over the $y$-axis. Draw the line of reflection and the image triangle.

32. Name the transformation.

33. Name the transformation.

34. Graph the figure with vertices $(4,-4),(2,-2)$, $(-1,-5)$, and $(1,-7)$. Rotate the figure $180^{\circ}$ about the origin.

35. Name the transformation. (Preimages are unshaded; images are shaded.)

36. The hexagon shown below is equiangular. How many lines of symmetry does it have?

a. 2
b. 1
c. 3
d. 6
37. For the figure below, draw all the lines of symmetry. If there are none, write "none."

38. Which of the following letters (if drawn as simply as possible) has at least one line of symmetry?
$\mathbf{Q}, \mathbf{S}, \mathbf{T}, \mathbf{Z}$
a. $\mathbf{S}$
b. $\mathbf{T}$
c. $\mathbf{Q}$
d. $\mathbf{Z}$
39. How many lines of symmetry does a regular hexagon have? Sketch the symmetry lines on the figure below.

40. How many lines of symmetry does an isosceles right triangle have? Draw a diagram to illustrate.
41. Does the clock face below have any rotational symmetry? If so, list any angles of rotation, $180^{\circ}$ or less, that can map it onto itself.

42. Tell whether the figure has rotational symmetry. If so, give each angle and direction of rotation that produces rotational symmetry.

43. Given $R P=22, R A=6$, and $\overline{P Q}$ is tangent to $\odot R$ at $Q$, find $P Q$.

44. Given $\overline{S T}$ is tangent to $\odot R$ at $S$, find $R T$.

45. Given: In $\odot O, m \overparen{B A C}=320^{\circ}$. Find $m \angle \mathrm{~A}$.

a. $26^{\circ}$
b. $13^{\circ}$
c. $20^{\circ}$
d. $10^{\circ}$
46. Given: In $\odot O, m \overparen{B A C}=298^{\circ}$. Find $m \angle B$.

a. $37^{\circ}$
b. $31^{\circ}$
c. $15.5^{\circ}$
d. $18.5^{\circ}$
47. Find the value of $x$.

a. $\quad 10.0$
b. 14.8
c. 11.3
d. 17.1
48. Given circle $O$ with radius 34 and $O C=16$. Find the length of $\overline{A B}$.

49. Given circle $O$ with radius 25 and $O C=7$. Find the length of $\overline{A B}$.

50. Find the value of $x$ to the nearest tenth.

51. Find $m \angle P S Q$ if $m \angle P S Q=3 y-5$ and $m \angle P R Q=$ $2 y+15$.

a. $27.5^{\circ}$
b. $20^{\circ}$
c. $55^{\circ}$
d. $35^{\circ}$
52. Given $\odot Q$ and $m \angle B=62^{\circ}$, find $m \overparen{A C}$.

53. Find the value of $x$ if $m \overparen{A B}=20^{\circ}$ and $m \overparen{C D}=62^{\circ}$.

a. $41^{\circ}$
b. $21^{\circ}$
c. $43^{\circ}$
d. $20.5^{\circ}$
54. Find the measure of $\angle 1$.

55. Find the measure of $\angle 1$.

56. Find the measure of $\angle 1$.

57. Find the value of $x$.

a. 18
b. 12
c. 6
d. 9
58. Find the value of $x$.

a. 24
b. 12
c. 18
d. 9
59. Find the value of $x$.

a. 8
b. 6
c. 3
d. none of these
60. Find the value of $x$.

a. 15
b. 8
c. none of these
d. 35

35
62. Find the area (not drawn to scale):

63. The area of the parallelogram is $\qquad$ .

64. Find the area of the region shown by dividing it into two trapezoids.

65. Find the area:

66. Find the area of the quadrilateral.

67. Circle $O$ has a radius of 7.39. If $m \angle A O B$ is $112^{\circ}$, then find the length of $\overparen{A B}$ to one decimal place.

68. Find the arc length of $\overparen{A B}$ to two decimal places.

69. Find the area of the shaded region. (Assume that the ends of the figure are semicircles.)

70. Find the area of the shaded region. Use $\pi \approx 3.14$.

71. Each circle is tangent to the other two. If the diameter of the large circle is 12 , the area of the shaded region is $\qquad$ .

a. $\quad 9 \pi$ sq. units
b. $36 \pi$ sq. units
c. $\quad 18 \pi$ sq. units
d. $24 \pi$ sq. units
72. Find the area of the shaded region.

a. $\quad 123.15 \mathrm{~cm}^{2}$
b. $\quad 38.48 \mathrm{~cm}^{2}$
c. $\quad 153.94 \mathrm{~cm}^{2}$
d. $\quad 30.79 \mathrm{~cm}^{2}$
73. Find the area of a regular heptagon with side length 10 cm .
a. $\quad 363.4 \mathrm{~cm}^{2}$
b. $\quad 346.7 \mathrm{~cm}^{2}$
c. $\quad 403.3 \mathrm{~cm}^{2}$
d. $726.8 \mathrm{~cm}^{2}$
74. Find the surface area of the right prism below.

75. The right prism below has bases which are equilateral triangles of side length 4 cm . Its height is 5 cm . Find its surface area.

76. Find the surface area of the cylinder to the nearest square unit. Use $\pi \approx 3.14$.

a. $\quad 98 \mathrm{~m}^{2}$
b. $\quad 307 \mathrm{~m}^{2}$
c. $62 \mathrm{~m}^{2}$
d. $614 \mathrm{~m}^{2}$
77. The surface area, in square centimeters, of the right cylinder below is $\qquad$ .

a. $\left(7^{2}\right) \pi+14 \pi(12)=217 \pi$
b. $\quad 14 \pi(12)=168 \pi$
c. $98 \pi+(14 \pi) 12=266 \pi$
d. $\left(7^{2} \pi\right)(12)=588 \pi$
78. Name the three dimesional solid which can be formed by this net.

a. Triangular Prism
b. Rectangular Prism
c. Triangular Pyramid
d. Rectangular Pyramid
79. Sketch a net for the solid.

80. The pyramid shown has a square base and a slant height of 7 ft . Find its surface area.

81. The surface area of the right cone shown is

a. $44 \pi$ in. ${ }^{2}$
b. $\quad 112 \pi$ in. ${ }^{2}$
c. $\quad 16 \sqrt{33} \pi$ in. ${ }^{2}$
d. $36 \pi$ in. ${ }^{2}$
82. Find the volume of the right triangular prism.

a. $\quad 60 \mathrm{~m}^{3}$
b. $288 \mathrm{~m}^{3}$
c. $576 \mathrm{~m}^{3}$
d. $36 \mathrm{~m}^{3}$
83. The volume of the right circular cylinder is about

a. $\quad 265.5 \mathrm{~m}^{3}$
b. $\quad 326.7 \mathrm{~m}^{3}$
c. $\quad 1036.9 \mathrm{~m}^{3}$
d. $\quad 1061.9 \mathrm{~m}^{3}$
84. A concrete block has a cylindrical hole 4 feet in diameter drilled through it to allow a pipe to pass through. How many cubic feet of concrete are left in the block? Use 3.14 as an approximation for $\pi$ and round your answer to the nearest tenth.

a. $\quad 90.0$ cubic feet
b. 85.4 cubic feet
c. 140.6 cubic feet
d. 203.4 cubic feet
85. The pyramid shown has a rectangular base and faces that are isosceles triangles. Find its volume.

86. Calculate the volume of the cone. Use $\pi \approx 3.14$.

a. $\quad 301.44 \mathrm{~m}^{3}$
b. $\quad 904.32 \mathrm{~m}^{3}$
c. $37.68 \mathrm{~m}^{3}$
d. $96 \mathrm{~m}^{3}$
87. Find the volume of the figure to the nearest tenth.

88. What is the volume of a sphere with diameter 9.4 feet?
a. $\quad 434.9 \mathrm{ft}^{3}$
b. $\quad 277.6 \mathrm{ft}^{3}$
c. $\quad 69.4 \mathrm{ft}^{3}$
d. $\quad 92.5 \mathrm{ft}^{3}$

Geometry Second Semester Final Exam Review
Answer Section

1. 9.592
2. D
3. $\sqrt{180} \mathrm{ft} ; 13.416 \mathrm{ft}$
4. C
5. $a=18, b=36 \sqrt{2}, h=12 \sqrt{2}$
6. 6
7. D
8. $a=8$
9. $x=5 \sqrt{3}, y=10$
10. $x=11, y=11 \sqrt{3}$
11. $x=4 \sqrt{2}$
12. $\frac{7}{24}$
13. Using the tangent ratio $\tan A=\frac{\text { leg opposite } \angle A}{\text { leg adjacent to } \angle A}$, $\tan 35^{\circ}=\frac{h}{150}$. So $h=150\left(\tan 35^{\circ}\right) \approx 150(0.7)$, or about 105 ft .
14. B
15. $\sin P=\frac{8}{17}, \cos P=\frac{15}{17}, \tan P=\frac{8}{15}$
16. A. $\frac{a}{c} \quad$ B. $\frac{b}{a} \quad$ C. $\frac{b}{c}$
17. 43 m
18. B
19. D
20. 5
21. 10.07
$\beta=70^{\circ}$
22. $b \approx 54.95$

$$
c \approx 58.48
$$

23. C
24. D
25. About $72.5^{\circ} \cdot \cos x=\frac{1500}{5000}$ so $x=\cos ^{-1}\left(\frac{1500}{5000}\right) \approx 72.5^{\circ}$
26. $x \approx 35 \mathrm{ft}$
27. $(13,-8)$
28. $(-2,-4)$
29. A
30. $(-x, y)$
31. $(y, x)$
32. 


33. Reflection
34. Reflection
35.

36. Translation
37. A

38.
39. B
40. 6

41. 1; diagrams should show the line of symmetry from the midpoint of the hypotenuse to the opposite vertex.
42. Yes, $180^{\circ}$.
43. yes; $120^{\circ}$ in either direction
44. $\sqrt{448}=8 \sqrt{7} \approx 21.2$
45. $\sqrt{425}=5 \sqrt{17} \approx 20.6$
46. C
47. B
48. A
49. 60
50. 48
51. 3
52. C
53. B
54. A
55. $56^{\circ}$
56. $32^{\circ}$
57. $68^{\circ}$
58. D
59. D
60. B
61. A
62. $16.15 \mathrm{~cm}^{2}$
63. A
64. 459 sq. units
65. 216 in. $^{2}$
66. 20 sq. units
67. 14.4 units
68. 2.62 cm
69. $\approx 322$ sq. units
70. $33.49 \mathrm{~cm}^{2}$
71. C
72. D
73. A
74. 54 in. ${ }^{2}$
75. $(60+8 \sqrt{3}) \mathrm{cm}^{2} \approx 73.9 \mathrm{~cm}^{2}$
76. D
77. C
78. B

79.
80. $95 \mathrm{ft}^{2}$
81. A
82. B
83. D
84. C
85. $32 \mathrm{ft}^{3}$
86. A
87. $418.9 \mathrm{~mm}^{3}$
88. A

